

من العلاقة ①

$$p(v-b) = nT \exp\left(-\frac{a}{nTV}\right)$$

$$pV = nT \exp\left(-\frac{a}{nTV}\right) + bp$$

$$= nT \left[\exp\left(-\frac{a}{nTV}\right) + \frac{b}{nT} p \right]$$

ولدينا ①

$$p = \frac{nT}{v-b} \exp\left(-\frac{a}{nTV}\right)$$

فيكون

$$pV = nT \left[\frac{1}{1-\frac{b}{v}} + \frac{b}{v-b} \right] \exp\left(-\frac{a}{nTV}\right)$$

التسلسل الجبري لـ

$$\exp(x) \approx 1 - x + \frac{x^2}{2} + \dots$$

$$pV = nT \left[1 + \frac{b}{v(1-\frac{b}{v})} \right] \left[1 - \frac{a}{nTV} + \frac{a^2}{2n^2T^2V^2} + \dots \right]$$

$$= nT \left[1 + \frac{b}{v} \left(1 + \frac{b}{v} \right) \right] \left[1 - \frac{a}{nTV} + \frac{a^2}{2n^2T^2V^2} + \dots \right]$$

$$= nT \left[1 + \frac{1}{v} \left(b - \frac{a}{nT} \right) + \frac{1}{v^2} \left(b^2 + \frac{a^2}{2n^2T^2} - \frac{ab}{nT} \right) + \dots \right]$$

$$= nT \left[1 + \frac{1}{v} \left(b - \frac{a}{nT} \right) + \frac{1}{v^2} \left(b^2 + \frac{a}{nT} \left(\frac{a}{2nT} - b \right) \right) + \dots \right]$$